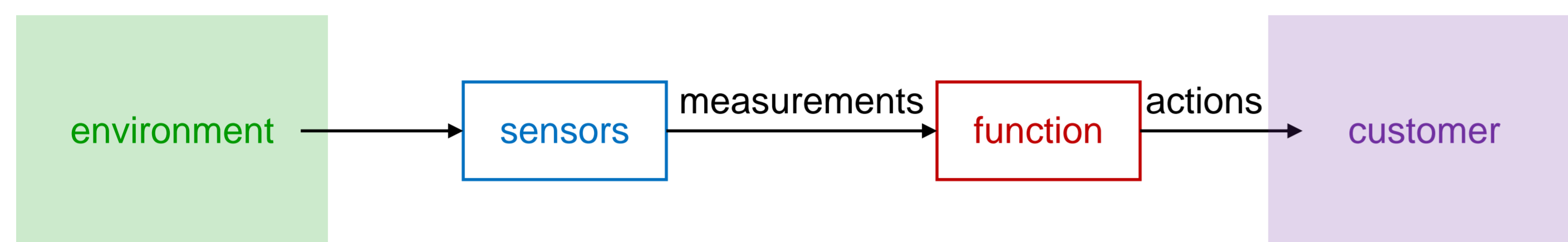


Robust Design of Sensors and Functions in Vehicular Safety

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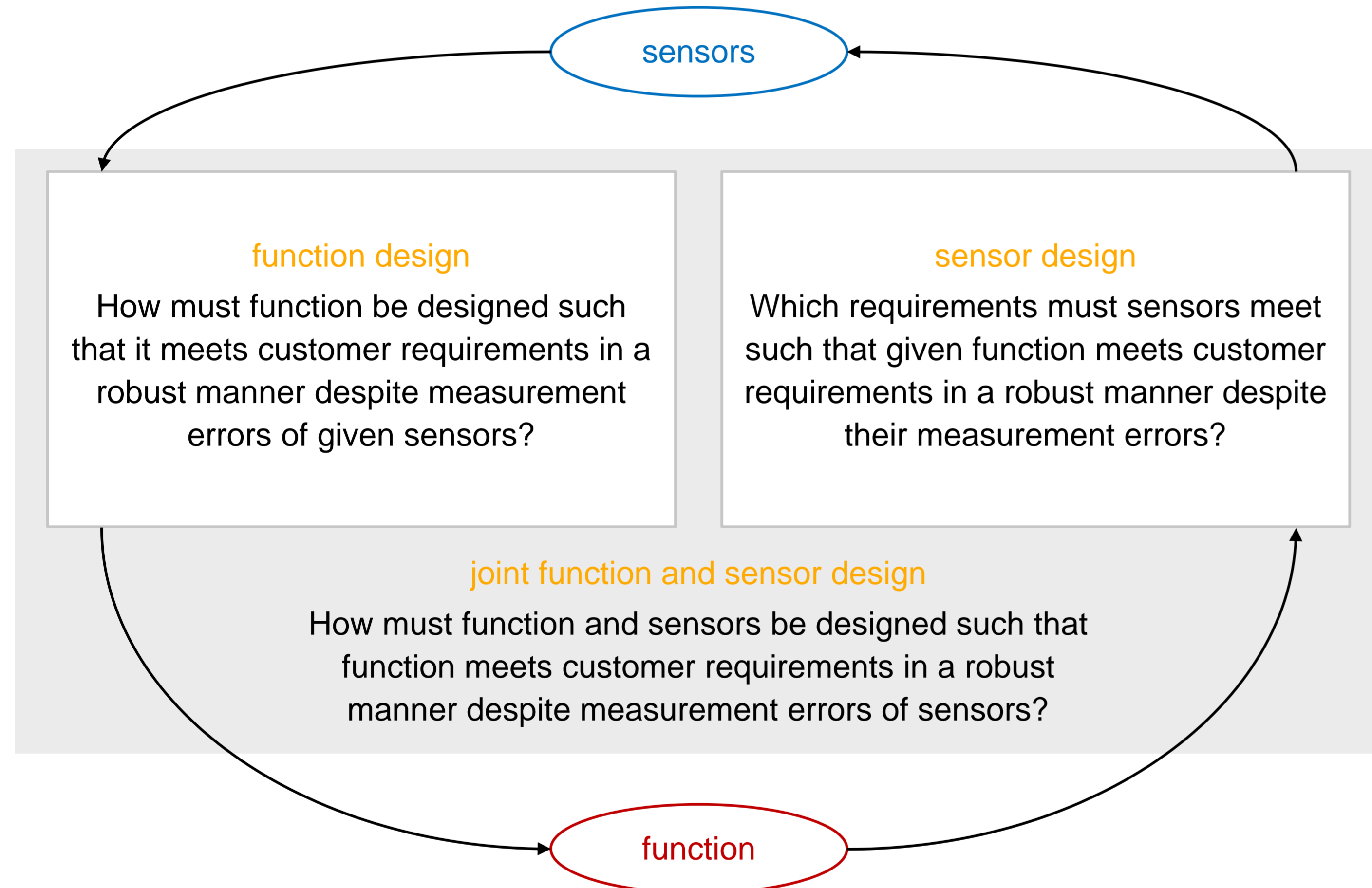
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Motivation



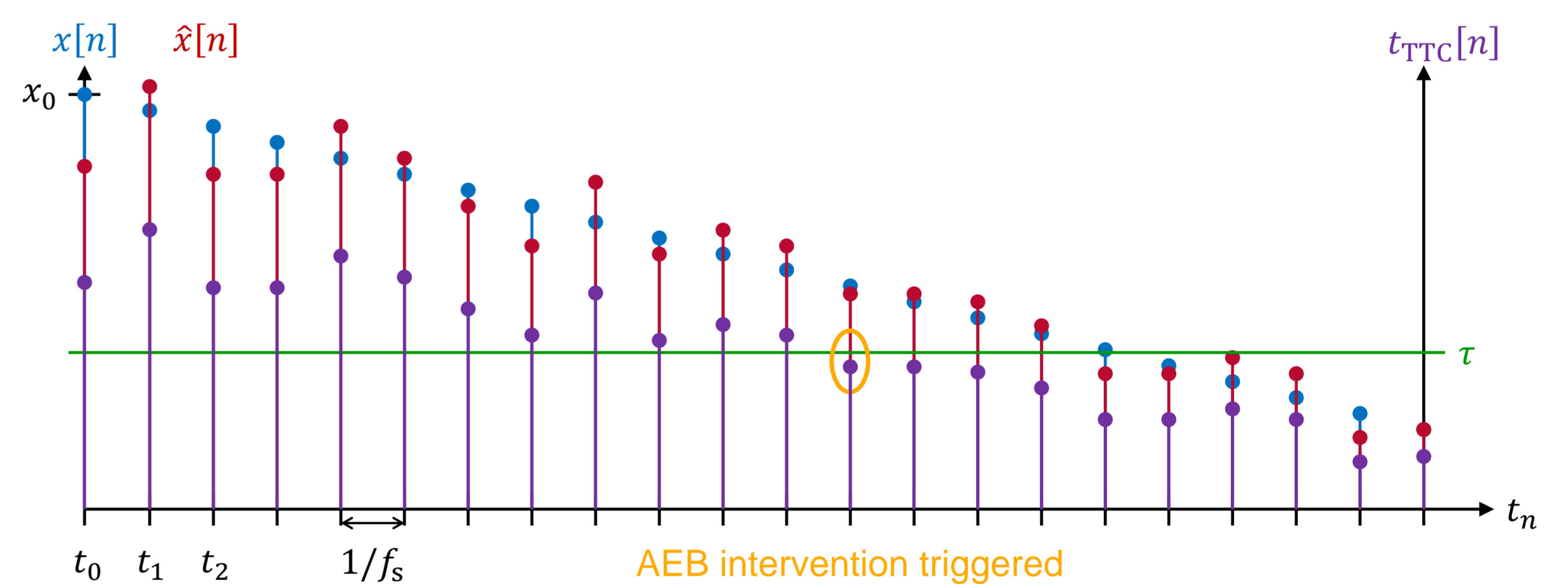
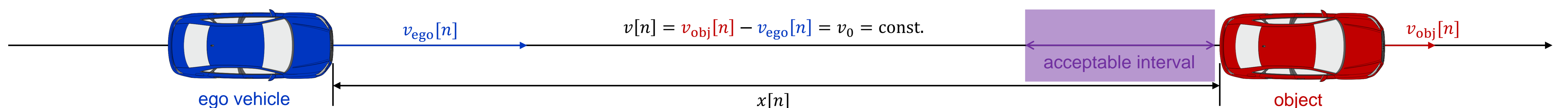
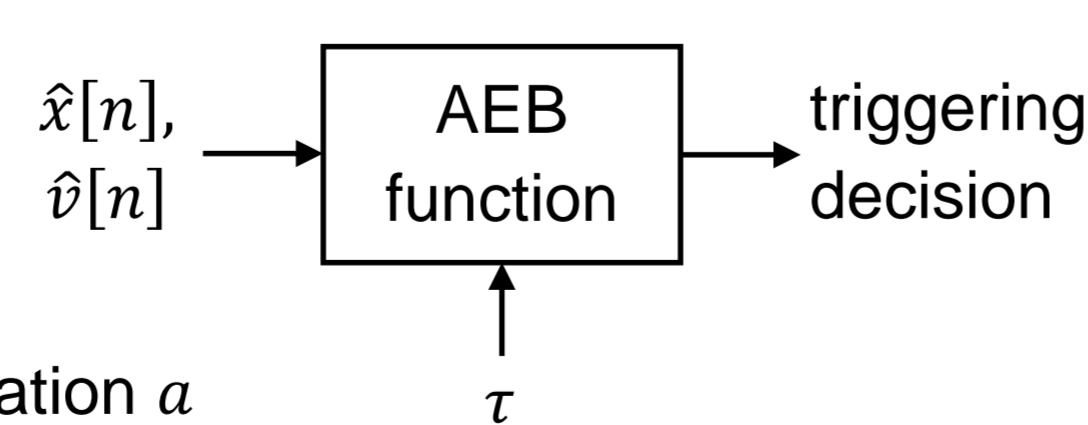
- **sensors:**
 - measure quantities like distances, velocities, accelerations, etc.
 - serve perception of environment of vehicle
- **(vehicular safety) function:**
 - uses measurements of sensors
 - interprets driving situation
 - triggers actions in dangerous situations like automatic emergency braking (AEB)
- problem: measurements of sensors are erroneous
- goal: function meets customer requirements in a robust manner despite measurement errors

Problem Formulation



Mathematical Model for Design of AEB System

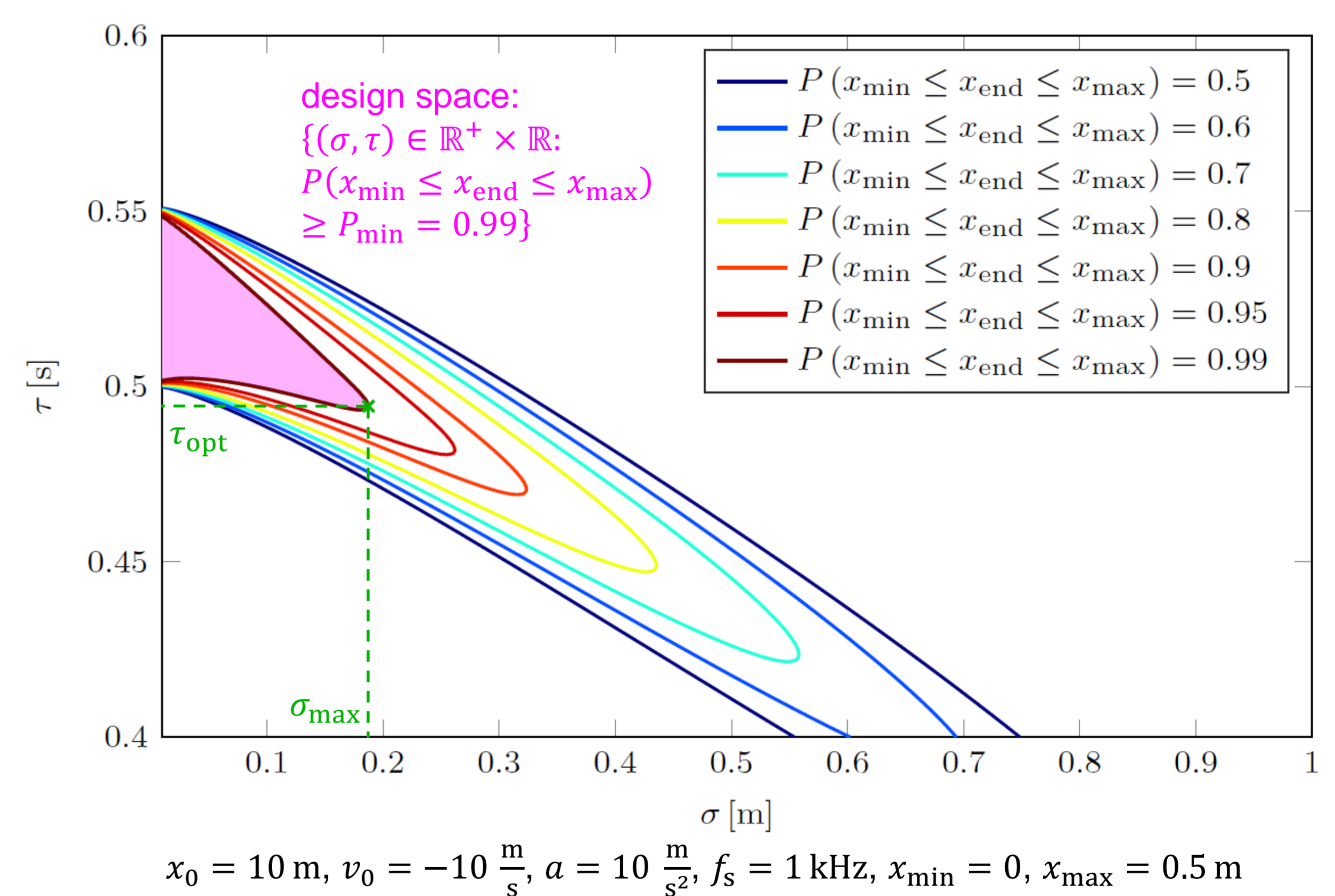
- state: $x[n] = \begin{bmatrix} x[n] \\ v[n] \end{bmatrix}$
- measurement: $y[n] = \begin{bmatrix} \hat{x}[n] \\ \hat{v}[n] \end{bmatrix}$
 - obtained by sensors with sampling rate f_s at $t_n = n/f_s, n \in \mathbb{N}_0$
 - measured distance: $\hat{x}[n] = x[n] + \epsilon[n]$, i.i.d. $\epsilon[n] \sim \mathcal{N}(0, \sigma^2)$
 - measured relative velocity: $\hat{v}[n] = v[n]$
- predicted time-to-collision (TTC): $t_{TTC}[n] = -\frac{\hat{x}[n]}{\hat{v}[n]}$
- AEB intervention
 - triggered by function at time instant t_n if $t_{TTC}[n] \leq \tau$ with threshold τ
 - reduces velocity of ego vehicle with constant deceleration a



Joint Function and Sensor Design for AEB System

$$(\sigma_{\max}, \tau_{\text{opt}}) = \underset{\sigma \in \mathbb{R}^+, \tau \in \mathbb{R}}{\text{argmax}} \sigma \quad \text{s.t.} \quad P(x_{\min} \leq x_{\text{end}} \leq x_{\max}) \geq P_{\min}$$

- $P(x_{\min} \leq x_{\text{end}} \leq x_{\max})$: probability that distance x_{end} from object after AEB intervention when relative velocity vanishes lies in acceptable interval $[x_{\min}, x_{\max}]$ (quality measure)
- P_{\min} : required minimum probability for fulfilling specification $x_{\min} \leq x_{\text{end}} \leq x_{\max}$
- σ_{\max} : maximal tolerable standard deviation of sensor measurement errors
- τ_{opt} : optimal threshold of function



Conclusion

- new methodology for robust design of AEB system considering sensor measurement errors
- future work: transfer of developed design methodology to further vehicular safety systems

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